

Mark Scheme (Provisional)

Summer 2021

Pearson Edexcel International GCSE
In Further Pure Mathematics (4PM1)
Paper 02

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the last candidate in exactly the same way as they mark the first.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification/indicative content will not be exhaustive.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, a senior examiner must be consulted before a mark is given.
- Crossed out work should be marked **unless** the candidate has replaced it with an alternative response.

Types of mark

- o M marks: method marks
- o A marks: accuracy marks
- o B marks: unconditional accuracy marks (independent of M marks)

Abbreviations

- o cao correct answer only
- o ft follow through
- o isw ignore subsequent working
- o SC special case
- oe or equivalent (and appropriate)
- o dep dependent
- o indep independent
- o awrt answer which rounds to
- o eeoo each error or omission

No working

If no working is shown then correct answers normally score full marks
If no working is shown then incorrect (even though nearly correct) answers score
no marks.

With working

If the final answer is wrong, always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

If a candidate misreads a number from the question. Eg. Uses 252 instead of 255; method marks may be awarded provided the question has not been simplified. Examiners should send any instance of a suspected misread to review.

If there is a choice of methods shown, then award the lowest mark, unless the answer on the answer line makes clear the method that has been used.

If there is no answer achieved then check the working for any marks appropriate from the mark scheme.

• Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

• Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded to another.

General Principles for Further Pure Mathematics Marking

(but note that specific mark schemes may sometimes override these general principles)

Method mark for solving a 3 term quadratic equation:

1. Factorisation:

$$(x^2+bx+c)=(x+p)(x+q)$$
, where $|pq|=|c|$ leading to $x=...$
 $(ax^2+bx+c)=(mx+p)(nx+q)$ where $|pq|=|c|$ and $|mn|=|a|$ leading to $x=...$

2. Formula:

Attempt to use the **correct** formula (shown explicitly or implied by working) with values for a, b and c, leading to x = ...

3. Completing the square:

$$x^{2} + bx + c = 0$$
: $(x \pm \frac{b}{2})^{2} \pm q \pm c = 0$, $q \ne 0$ leading to $x = ...$

Method marks for differentiation and integration:

1. <u>Differentiation</u>

Power of at least one term decreased by 1. $(x^n \rightarrow x^{n-1})$

2. Integration:

Power of at least one term increased by 1. $(x^n \rightarrow x^{n+1})$

Use of a formula:

Generally, the method mark is gained by **either**

quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values

or, where the formula is <u>not</u> quoted, the method mark can be gained by implication from the substitution of <u>correct</u> values and then proceeding to a solution.

Answers without working:

The rubric states "Without sufficient working, correct answers may be awarded no marks".

General policy is that if it could be done "in your head" detailed working would not be required. (Mark schemes may override this eg in a case of "prove or show...."

Exact answers:

When a question demands an exact answer, all the working must also be exact. Once a candidate loses exactness by resorting to decimals the exactness cannot be regained.

Rounding answers (where accuracy is specified in the question)

Penalise only once per question for failing to round as instructed - ie giving more digits in the answers. Answers with fewer digits are automatically incorrect, but the isw rule may allow the mark to be awarded before the final answer is given.

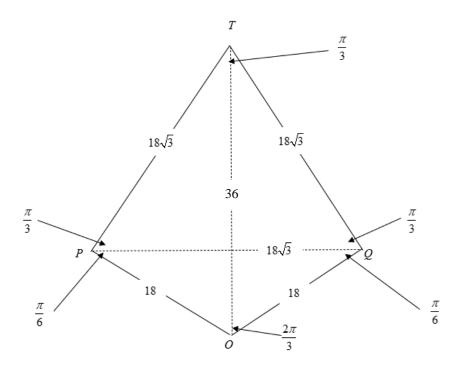
| Paper 1 | | |
|----------|--|---------------|
| Question | Scheme | Marks |
| number | | |
| 1 (a) | 3x < 12 | M1 |
| | x < 4 | A1 |
| | | [2] |
| (b) | (2x+1)(x-3) > 0 | M1 |
| | $(2x+1)(x-3) > 0$ Critical values are $x = -\frac{1}{2}$ and $x = 3$ | M1 |
| | $x < -\frac{1}{2}$ $x > 3$ | A1 |
| | | [3] |
| (c) | $x < -\frac{1}{2} 3 < x < 4$ | B1ft |
| | 2 | [1] |
| | | Total 6 marks |

| Part | Mark | Guidance | | | |
|------------|-----------|---|--|--|--|
| (a) | M1 | Attempts to solve the inequality to achieve $3x < 12$ | | | |
| | 1411 | Allow $3x < a$ where a is an integer | | | |
| | A1 | For $x < 4$ | | | |
| (b) | | Attempts to solve the inequality by any method to find critical values | | | |
| | | See General Guidance for acceptable methods. | | | |
| | | If a calculator is used, the solution must be fully correct for this mark. | | | |
| | M1 | Allow = or > for this mark or even no sign at all provided it is clear they are solving a quadratic. | | | |
| | | $(2x+1)(x-3) > 0 \Rightarrow x =, \left(x = -\frac{1}{2}, 3\right)$ | | | |
| | M1 | For forming a correct inequality, which must be an open interval, following through their two critical values which must have come from the solution of a 3TQ. $x < -\frac{1}{2} x > 3$ Accept any correct notation. E.g., $x < -\frac{1}{2}$ or $x > 3$ Or $\left\{x: x < -\frac{1}{2}\right\} \cup \left\{x: x > 3\right\}$ | | | |
| | | Condone $x < -\frac{1}{2}$ and $x > 3$ for this mark only | | | |
| | A1 | For the correct inequality with the correct critical values using any acceptable notation. Eg, $x < -\frac{1}{2}$ $x > 3$ | | | |
| (c) | | Eg, $x < -\frac{1}{2}$ $x > 3$ For $x < -\frac{1}{2}$ $3 < x < 4$ | | | |
| | B1ft | ft their answers from parts (a) and (b) provided (b) is of the form $x < p$ and/or $x > q$ | | | |

| Question number | Scheme | Marks |
|--------------------|--|--------------------|
| 2 (a) | $2 - \frac{1}{25} (x^2 - 20x)$ | |
| | $2 \mp \frac{1}{25} \Big[(x \pm 10)^2 - 100 \Big]$ | M1 |
| ALT | $6 - \frac{1}{25}(x - 10)^2$ So $A = 6$ $B = \frac{1}{25}$ $C = -10$ | A1 A1 A1 (4) |
| ALI | $A - Bx^2 - 2BCx - BC^2 = 2 + \frac{4}{5}x - \frac{1}{25}x^2$ | {M1} |
| | $B = \frac{1}{25}$ | {A1} |
| | $-\frac{2}{25}C = \frac{4}{5} \qquad C = -10$ | {A1} |
| | $-\frac{1}{25}(100) + A = 2 \qquad A = 6$ | {A1} (4) |
| (b)(i) | 6 | B1 ft |
| (b)(ii) | 10 | B1 ft (2) |
| | To | otal 6 marks |

| Part | Mark | Guidance | | |
|--------|-----------|--|--|--|
| (a) | M1 | For a complete method to complete the square to achieve as a minimum | | |
| | | $2 \mp \frac{1}{25} (x \pm 10)^2 - p$ or $\mp \frac{1}{25} [(x \pm 10)^2 - q - 50]$ | | |
| | | where p and q are constants | | |
| | A1 | For one correct from $A = 6$ $B = \frac{1}{25}$ or $C = -10$ whether stated | | |
| | | explicitly or embedded | | |
| | A1 | For two correct from $A = 6$ $B = \frac{1}{25}$ or $C = -10$ whether stated | | |
| | | explicitly or embedded | | |
| | A1 | Fully correct $A = 6$ $B = \frac{1}{25}$ and $C = -10$ OR $6 - \frac{1}{25}(x - 10)^2$ oe | | |
| | ALT – | equates coefficients | | |
| | M1 | For an attempt to expand $A - B(x+C)^2$ AND equate coefficients to the | | |
| | | given $f(x) \Rightarrow A - Bx^2 - 2BCx - BC^2 = 2 + \frac{4}{5}x - \frac{1}{25}x^2$ | | |
| | | Allow $A \pm Bx^2 \pm 2BCx \pm BC^2$ for the expansion of $A - B(x+C)^2$ | | |
| | | There must be an attempt to equate at least one coefficient. | | |
| | | $-B = -\frac{1}{25} \Longrightarrow B = \dots$ | | |
| | | $-2BC = \frac{4}{5} \Rightarrow C = \dots$ | | |
| | | $A - BC^2 = 2 \Longrightarrow A = \dots$ | | |
| | A1 | For one correct from $A = 6$ $B = \frac{1}{25}$ or $C = -10$ whether stated | | |
| | | explicitly or embedded | | |
| | A1 | For two correct from $A = 6$ $B = \frac{1}{25}$ or $C = -10$ whether stated | | |
| | | explicitly or embedded | | |
| | A1 | Fully correct $A = 6$ $B = \frac{1}{25}$ and $C = -10$ OR $6 - \frac{1}{25}(x - 10)^2$ oe | | |
| (b)(i) | B1ft | For the value of 6 or ft their A | | |
| (ii) | B1ft | For the value of 10 or ft their C | | |

| Question number | Scheme | Marks |
|--------------------|---|-----------|
| 3 (a) | $PQ = 18 \times \frac{2}{3}\pi = 12\pi$ | M1 A1 (2) |
| (b)(i) | $\alpha = \frac{1}{3}\pi$ | B1 |
| (b)(11) | $PT = 18\tan\frac{\pi}{3} = 18\sqrt{3}$ | M1 A1 |
| | Area of $OPTQ = 2 \times \frac{1}{2} \times 18 \times 18\sqrt{3}$ | M1 |
| | Area of Sector $OPQ = \frac{1}{2} \times 18^2 \times \frac{2\pi}{3}$ | M1 |
| | Shaded Area = $2 \times \frac{1}{2} \times 18 \times 18\sqrt{3} - \frac{1}{2} \times 18^2 \times \frac{2\pi}{3} = 222 \text{ cm}^2$ | M1 A1 (7) |
| | Tota | l 9 marks |



Area of triangle $OPQ = 81\sqrt{3}$ or 140.29... cm²

Area of triangle $PQT = 243\sqrt{3}$ or 420.88... cm²

Area of quadrilateral $OTPQ = 324\sqrt{3}$ or 561.18... cm²

| Part | Mark | Guidance |
|------|-----------|--|
| (a) | M1 | Uses the correct formula for the length of arc to give $PQ = 18 \times \frac{2}{3} \pi = \dots$ |
| | A1 | For $PQ = 12\pi$ |

| | ALT – | ALT – works in degrees (but the angle must be correct at 120°) | | | |
|------|------------------|--|--|--|--|
| | | Uses the correct formula for length of arc to give $PQ = \frac{120}{360} \times 2\pi \times 18 = \dots$ | | | |
| | M1 | | | | |
| | | | | | |
| (1-) | A1 | For $PQ = 12\pi$ | | | |
| (b) | (i) B1 | For stating $\alpha = \frac{\pi}{3}$ (Please check the diagram as it may written on there) | | | |
| | (ii) Me correct. | | | | |
| | | $\left(\angle POQ = 120^{\circ}, \ \angle PTQ = 60^{\circ}\right)$ | | | |
| | Finds l | ength of PT | | | |
| | | For finding length <i>PT</i> : e.g., | | | |
| | M1 | $\tan\left(\frac{\pi}{3}\right) = \frac{PT}{18} \Rightarrow PT = 18\tan\left(\frac{\pi}{3}\right) = \dots$ | | | |
| | | The given values must be used correctly | | | |
| | A1 | For $PT = 18\sqrt{3}$ | | | |
| | M1 | For the area of $OPTQ = 2 \times \frac{1}{2} \times 18 \times '18 \sqrt{3}' = (561.18)$ | | | |
| | | Their $18\sqrt{3}$ must come from an attempt at using trigonometry. | | | |
| | Method | | | | |
| - | Finds le | engths PQ and TO | | | |
| | | For finding the lengths PQ and TO using any acceptable correct trigonometry. | | | |
| | M1 | e.g., $PQ = \sqrt{18^2 + 18^2 - 2 \times 18 \times 18 \cos\left(\frac{2\pi}{3}\right)} = \dots$ and $TO = \frac{\cos\left(\frac{\pi}{3}\right)}{18} = \dots$ | | | |
| - | | The given values must be used correctly | | | |
| | A1 | For both correct lengths: $PQ = 18\sqrt{3}$ and $TO = 36$ | | | |
| | M1 | For the area of $OPTQ = \frac{1}{2} \times '18\sqrt{3}' \times '36' = (561.18)$ Their $18\sqrt{3}$ and 36 must come from an attempt at using | | | |
| | | trigonometry | | | |
| | | $1 	 2\pi$ | | | |
| | | For the area of sector $OPQ = \frac{1}{2} \times 18^2 \times \frac{2\pi}{3} = (339.29)$ | | | |
| | M1 | or $\frac{120^{\circ}}{360^{\circ}} \times \pi \times 18^2 = (339.29)$ | | | |
| | M1 | For area of <i>OPTQ</i> – area of Sector <i>OPQ</i> | | | |
| | | 561.18 – 339.29 = 221.887 | | | |
| | A1 | 561.18 - 339.29 = 221.887 For 222 cm ² (must be 3sf) (Units are not required) | | | |

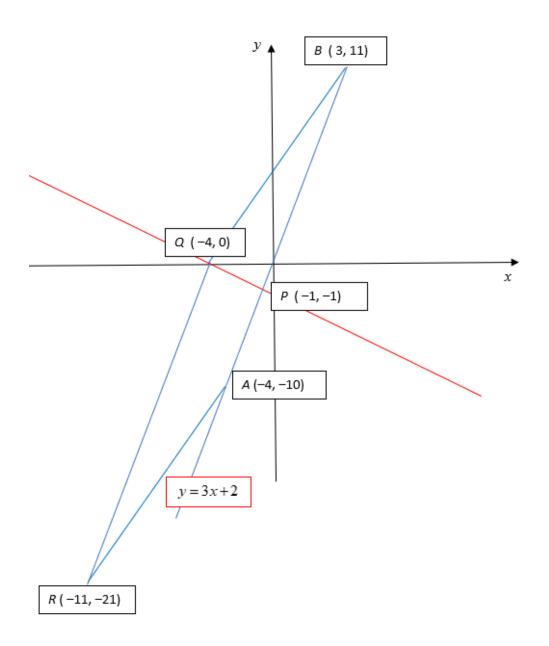
| Question number | Scheme | Marks |
|--------------------|---|--------------------|
| 4 (a) | Gradient = $\frac{11+10}{3+4}$ = 3 | |
| | y+10=3(x+4) or $y-11=3(x-3)$ oe | M1A1 (2) |
| (b) | e.g. $\left(\frac{4 \times -4 + 3 \times 3}{3 + 4}, \frac{4 \times -10 + 3 \times 11}{3 + 4}\right) = (-1, -1)$ | M1 A1 (2) |
| ALT (b) | Using Vectors $\begin{pmatrix} -4 \\ -10 \end{pmatrix} + \frac{3}{7} \begin{pmatrix} 7 \\ 21 \end{pmatrix} = \begin{pmatrix} -1 \\ -1 \end{pmatrix} \text{or} \begin{pmatrix} 3 \\ 11 \end{pmatrix} - \frac{4}{7} \begin{pmatrix} 7 \\ 21 \end{pmatrix} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$ | {M1} {A1} |
| (c) | $-\frac{1}{3} = \frac{n+1}{m+1} \Longrightarrow -\frac{1}{3}(m+1) = n+1$ | M1 |
| | $\left(\sqrt{10}\right)^2 = \left(m+1\right)^2 + \left(n+1\right)^2$ | M1 |
| | $10 = (m+1)^2 + \frac{1}{9}(m+1)^2$ | M1 |
| | $9 = (m+1)^{2}$ $m = -4 \qquad n = 0$ | M1 A1 A1 (6) |
| ALT (c) | Using Vectors $\overrightarrow{AB} = \begin{pmatrix} 7 \\ 21 \end{pmatrix}$ so perpendicular to $\overrightarrow{AB} = \begin{pmatrix} 21 \\ -7 \end{pmatrix}$ | {M1} |
| | $\left \overrightarrow{AB} \right = 7\sqrt{10} \Rightarrow, \left \overrightarrow{AP} \right = 3\sqrt{10}$ | {M1,M1} |
| | $\overrightarrow{PQ} = \frac{\sqrt{10}}{7\sqrt{10}} \times \begin{pmatrix} 21\\ -7 \end{pmatrix} = \begin{pmatrix} 3\\ -1 \end{pmatrix}$ | {M1} |
| | So $Q = (-1 - 3, -11)$ | {A1} |
| | Q = (-4,0) | {A1} |
| (d)(i) | $AB = \sqrt{(3+4)^2 + (11+10)^2} = 7\sqrt{10}$ | M1 |
| | $RQ = \sqrt{(-11+4)^2 + (-21)^2} = 7\sqrt{10}$ | A1 |
| (d)(ii) | Gradient of $RQ = \frac{-21 - 0}{11 + 4} = 3$ | M1 |
| | -11 + 4 So Gradient of AB (=3) = Gradient of RQ | A1 (4) |

| ALT (d) | Using Vectors | |
|---------|---|--------------|
| | $\overrightarrow{RQ} = \begin{pmatrix} -4 - (-11) \\ 0 - (-21) \end{pmatrix} = \begin{pmatrix} 7 \\ 21 \end{pmatrix}$ | {M1} {A1} |
| | $\overrightarrow{AB} = \begin{pmatrix} 7 \\ 21 \end{pmatrix} = \overrightarrow{RQ}$ | {M1} |
| | Because the vectors are the same they must be parallel and the | {A1} |
| (e) | same length $Area = 7\sqrt{10} \times \sqrt{10} = 70$ | M1 A1 (2) |
| ALT (e) | Using Vectors | (-) |
| | Using Vectors $ \frac{1}{2} \begin{vmatrix} 3 & -4 & -11 & -4 & 3 \\ 11 & 10 & -21 & 0 & 11 \end{vmatrix} $ | {M1} |
| | = 70 | {A1} |
| | Total is | 16 marks |

| Part | Mark | Guidance | | | | |
|------------|--|--|--|--|--|--|
| (a) | M1 | For a fully correct method of finding an equation of a straight line. | | | | |
| | | $\frac{y - y_1}{y_2 - y_1} = \frac{x - x_1}{x_2 - x_1} \Rightarrow \frac{y - (-10)}{11 - (-10)} = \frac{x - (-4)}{3 - (-4)}$ | | | | |
| | | $y_2 - y_1 - x_2 - x_1 - 11 - (-10) - 3 - (-4)$ | | | | |
| | | Or finds gradient $\frac{11+10}{3+4} = 3$ and uses $y+10=3(x+4)$ or $y-11=3(x-3)$ | | | | |
| | | of $y = mx + c$ is used, they must find a complete equation for this mark. | | | | |
| | | Allow one error only for the award of this mark. | | | | |
| | A1 | For a correct line in any form. | | | | |
| | | y+10=3(x+4) or $y-11=3(x-3)$ | | | | |
| | | or $y = 3x + 2$ | | | | |
| | | or even $\frac{y+10}{21} = \frac{x+4}{7}$ but do not allow incomplete processing. | | | | |
| (b) | M1 | For one correct from $x = -1$ or $y = -1$ | | | | |
| | A1 | For the correct coordinates of point $P(-1,-1)$ | | | | |
| | | Accept $x = -1$ $y = -1$ | | | | |
| (c) | M1 | Uses the perpendicular gradient to set up an equation in m and n . | | | | |
| | | $-\frac{1}{3'} = \frac{n - (-1)'}{m - (-1)'} \Rightarrow -\frac{1}{3'}(m+1) = n+1 \text{ or } n = -\frac{1}{3}n + \frac{4}{3}$ | | | | |
| | | Ft their gradient in part (a) and their <i>P</i> from part (b) for this mark. | | | | |
| | M1 | Uses Pythagoras theorem to set up an equation in m and n . | | | | |
| | | $\left(\sqrt{10}\right)^2 = \left(m - '(-1)'\right)^2 + \left(n - '(-1)'\right)^2$ | | | | |
| | | Ft their coordinates of point <i>P</i> form part (b) for this mark. | | | | |
| | M1 | Attempts to solve their two equations in <i>n</i> and <i>m</i> simultaneously and forms a quadratic equation in one variable only. | | | | |
| | | $10 = (m+1)^2 + \frac{1}{9}(m+1)^2 \Rightarrow 9 = (m+1)^2 \text{ or } 0 = m^2 + 2m - 8$ | | | | |
| | | or $10 = 9(n+1)^2 + (n+1)^2 \Rightarrow 0 = 10n^2 + 20n$ | | | | |
| | M1 | For solving their either: $9 = (m+1)^2 \Rightarrow m =$ or $0 = 10n^2 + 20n \Rightarrow n =$ | | | | |
| | | which must be a quadratic equation. | | | | |
| | A1 | For finding either $m = -4$ or $n = 0$ | | | | |
| | A1 | Condone the sight of $m = 2$ for this mark. | | | | |
| | | For finding both $m = -4$ and $n = 0 \Rightarrow (-4, 0)$ | | | | |
| | AI.T = | The final answer must be given as coordinates. using vectors – see main scheme. | | | | |
| (d)(i) | ALI - | | | | | |
| (u)(1) | M1 | For finding either the length $AB = \sqrt{(3+4)^2 + (11+10)^2} = 7\sqrt{10}$ | | | | |
| | 1711 | Or $RQ = \sqrt{(-11+4)^2 + (-21)^2} = 7\sqrt{10}$ | | | | |
| | A1 | For finding both the length $AB = \sqrt{(3+4)^2 + (11+10)^2} = 7\sqrt{10}$ | | | | |
| | 144 | And $RQ = \sqrt{(-11+4)^2 + (-21)^2} = 7\sqrt{10}$ and states they are equal | | | | |
| (d)(ii) | M1 The gradient of $RQ = \frac{-21 - '0'}{-11 - '(-4)'} = '3'$ | | | | | |
| | | Ft their coordinates from part (c) | | | | |

| | A1 States that the gradient of RQ = gradient of AB [from (a)] | | | | | |
|--------|---|---|--|--|--|--|
| | A1 | States that the gradient of $NQ = \text{gradient of } AD \text{ [Holh (a)]}$ | | | | |
| | ALT · | – Uses vectors, see main scheme. Ft their coordinates of $Q - (m, n)$ | | | | |
| (e) | M1 | For a correct expression for the area using their length of AB and the given | | | | |
| | | length of PQ $(\sqrt{10})$ | | | | |
| | | Area = $7\sqrt{10} \times \sqrt{10} =$ | | | | |
| | A1 | For the area = 70 [square units] | | | | |
| | ALT | LT – Uses the discriminant | | | | |
| | M1 | For a correct expression of the area in sequential order using their | | | | |
| | | coordinates for Q | | | | |
| | | Area = $\frac{1}{2}\begin{vmatrix} 3 & -4 & -11 & '-4' & 3 \\ 11 & 10 & -21 & '0' & 11 \end{vmatrix}$ | | | | |
| | A 1 | | | | | |
| T. 6 1 | | A1 Area = 70 [square units] | | | | |

Useful sketch



| Question number | Scheme | Marks |
|--------------------|---|-----------|
| 5 (a) | $u_2 + u_4 = ar + ar^3 = 212.5$ | M1 |
| | $u_3 + u_4 = ar^2 + ar^3 = 62.5$ | |
| | $\frac{\left(1+r^2\right)}{\left(r+r^2\right)} = \frac{17}{5}$ | M1 |
| | $12r^2 + 17r - 5 = 0$ | M1 |
| | (4r-1)(3r+5)=0 | M1 |
| | $r = \frac{1}{4} \qquad r = -\frac{5}{3}$ | A1 (5) |
| (b) | $r = \frac{1}{4} \Rightarrow a = 800$ So $\frac{a}{1-r} = \frac{800}{3} = \frac{3200}{3}$ | |
| | $1-r \frac{3}{4}$ 3 | M1 A1 (2) |
| | Tota | l 7 marks |

| Part | Mark | Guidance | | |
|------------|---|--|--|--|
| (a) | M1 | For either $ar + ar^3 = 212.5$ or $ar^2 + ar^3 = 62.5$ correct | | |
| | | For either $ar + ar^3 = 212.5$ or $ar^2 + ar^3 = 62.5$ correct For attempting to eliminate a or ar either by division or substitution: | | |
| | M1 | e.g. $\frac{ar(1+r^2)}{ar(r+r^2)} = \frac{212.5}{62.5} \Rightarrow \frac{(1+r^2)}{(r+r^2)} = \frac{212.5}{62.5} = \left(\frac{17}{5}\right)$ | | |
| | Motho | An attempt involves some factorisation to eliminate <i>a</i> or <i>ar</i> d 1 – finds a 3TQ | | |
| | Metho | For forming a 3TQ in r only using their expressions. | | |
| | $(12r^2 + 17r - 5 = 0 \text{ oe})$ Accept for example $150r^2 + 212.5r - 62.5 = 0$ | | | |
| | | For an attempt to solve their 3TQ to give two values of r | | |
| | dM1 | See General Guidance for the definition of an attempt. | | |
| | | For example: $(4r-1)(3r+5) = 0 \Rightarrow r =,$ | | |
| | | This mark is dependent on the FIRST M mark being awarded | | |
| | Metho | d 2 – finds a cubic equation | | |
| | M1 | For forming a cubic with a common factor of r in each term. e.g. $12r^3 + 17r^2 - 5r = 0$ | | |
| | | For factorising their cubic equation to achieve $r(12r^2+17r-5)=0$ | | |
| | dM1 | and for an attempt to solve their 3TQ to give two values of r Ignore $r = 0$ if also given. See General Guidance for the definition of an attempt. For example: $(4r-1)(3r+5) = 0 \Rightarrow r =,$ | | |
| | | - | | |
| | | This mark is dependent on the FIRST M mark being awarded | | |
| | A1 | For the correct values; $r = \frac{1}{4}$ and $r = -\frac{5}{3}$ (reject $r = 0$ if seen earlier) | | |
| (b) | | Uses their $r = \frac{1}{4}$ [where $ r < 1$] to find the value of a (800) with the correct | | |
| | M1 | formula for the sum of a geometric series to infinity. Condone an incorrect value of a even if they have used $r = \frac{1}{4}$ [The formula is given on page 2 of this booklet]. | | |
| | | $S_{\infty} = \frac{a}{1-r} = \frac{'800'}{1-'\frac{1}{4}'} = \dots$ | | |
| | For the correct value, $S_{\infty} = \frac{3200}{3}$ or $1066\frac{2}{3}$ | | | |
| | | Do not accept for example 1066.67 unless the stated value is 1066.6 | | |

| Question number | Scheme | Marks |
|-----------------|---|----------|
| 6 (a) | f(3) = 27 + 9p + 9 - 30 + q = 0 | M1 A1 |
| | 9p + q + 6 = 0 * | A1 cso |
| | | (3) |
| (b) | $f(-p) = -p^3 + p^2(p+1) + 10p + q = 0$ | M1 A1 |
| | $p^2 + 10p + q = 0$ * | A1 cso |
| | | (3) |
| (c) | $p^2 + 10p - 9p - 6 = 0$ | M1 |
| | $p^2 + p - 6 = 0$ | A1 |
| | (p+3)(p-2) = 0 | M1 |
| | p=2 $q=-24$ | A1 A1 |
| | | (5) |
| (d) | (x+a)(x-3)(x+2) | |
| | So $-3 \times 2 \times a = -24$ $a = 4$ | M1 |
| | (x+4)(x-3)(x+2) | A1 |
| | | (2) |
| | Total | 13 marks |

| Part | Mark | Guidance | | | | | |
|------------|---|---|--|--|--|--|--|
| Gener | General guidance for marking parts (a) and (b) | | | | | | |
| • | • For the award of full marks in parts (a) and/or (b) you must see = 0 used in a line of working before the final answer. | | | | | | |
| • | which | ndidate does not use = 0 in either parts (a) or (b) [except in the final line – is a given answer] deduct the M mark (and the subsequent A marks) in only st occurrence of the absence. | | | | | |
| (a) | M1 | For using $f(\pm 3) = 0$ in the given equation set = 0 | | | | | |
| | A1 | For obtaining the correct unsimplified expression: $27 + 9p + 9 - 30 + q = 0$ | | | | | |
| | A1 | For obtaining the given equation $9p + q + 6 = 0*$ | | | | | |
| | cso | Note: This is a show question. There must be no errors seen. | | | | | |
| (b) | M1 | For use of $f(\pm p) = 0$ in the given equation set = 0 | | | | | |
| | A1 | For obtaining the correct unsimplified expression: | | | | | |
| | | $-p^3 + p^2(p+1) + 10p + q = 0$ | | | | | |
| | A1 | For obtaining the correct given equation $p^2 + 10p + q = 0$ * | | | | | |
| | cso | Note: This is a show question. There must be no errors seen. | | | | | |

| M1 | For attempting to solve the given two equations simultaneously to achieve | | | | |
|-----------|--|--|--|--|--|
| | a 3TQ in either p or q only. | | | | |
| | E.g. substitutes $q = \mp 9p \mp 6$ or $\left[p = \frac{\mp q \mp 6}{9} \text{ and } p^2 = \frac{(\mp q \mp 6)^2}{81}\right]$ into | | | | |
| | $p^2 + 10p + q = 0$ | | | | |
| | This mark may be implied by the correct 3TQ | | | | |
| A1 | For the correct 3TQ $p^2 + p - 6 = 0$ or $q^2 + 3q - 504 = 0$ | | | | |
| M1 | For an attempt to solve their 3TQ in either <i>p</i> or <i>q</i> using factorisation, use of the formula or completing the square. See general guidance for the definition of an attempt. For example: | | | | |
| | $(p+3)(p-2) = 0 \Rightarrow p = \dots$ or $(q+24)(q-21) = 0 \Rightarrow q = \dots$, | | | | |
| | If a candidate uses their calculator to solve their 3TQ, the final values must be correct for the award of this mark unless a valid method is seen. | | | | |
| A1 | For either the correct value of p OR the correct value of q | | | | |
| | p=2 or $q=-24$ | | | | |
| | Condone the presence $p = -3$, and/or $q = 21$ | | | | |
| A1 | For both the correct value of $p = 2$ AND the correct value of $q = -24$ Must reject $p = -3$, and/or $q = 21$ if seen. | | | | |
| M1 | [f(x) = (x+a)(x-3)(x+2')] | | | | |
| | For attempting to find the value of a | | | | |
| | $-3 \times '2' \times a = '-24' \Rightarrow a = \dots$ | | | | |
| | OR | | | | |
| | For an attempt using division with their values of p and q | | | | |
| | $x^2 - x - 6$ $x^3 + 3x^2 - 10x - 24$ | | | | |
| | Allow a quotient of $x+b$ where b is a constant. | | | | |
| A1 | For the correct factorised expression $(x+4)(x-3)(x+2)$ which must be | | | | |
| | written out in full on one line. | | | | |
| | A1 A1 A1 M1 | | | | |

| Question number | | | Scheme | | Marks |
|--------------------|---|----------------|--------|------|-----------|
| 7 (a) | 2 | 3 | 4 | | B1 B1 |
| | 3.73 | 4.28 | 5 | | (2) |
| (b) | Points plotte | d | | | B1ft |
| | Joined up wi | th a smooth o | curve | | B1ft |
| | | | | | (2) |
| (c) | $\log_{3}(6-2x)$ $6-2x = 3^{\frac{x}{4}}$ $8-2x = 3^{\frac{x}{4}}$ $y = 8-2x$ | $=\frac{x}{4}$ | | | M1 |
| | $6 - 2x = 3^{\frac{x}{4}}$ | | | | M1 |
| | $8 - 2x = 3^{-4}$ | + 2 | | | A1 |
| | y = 8 - 2x | drawn | | | M1 |
| | x = 2.1 | | | | A1 |
| | | | | | (5) |
| | | | | Tota | l 9 marks |

| Part | Mark | Guidance | | | | |
|------|-----------|--|--|----------------------|------------|--------------------------------|
| (a) | B1 | For two points (rounded correctly) correct from; | | | | |
| | | | | | | 1 |
| | | 0 1 | 2 | 3 | 4 | 5 |
| | | 3 3.32 3 | 3.73 | 4.28 | 5 | 5.95 |
| | | | | | | |
| | B1 | All three points correct and o | correctly | z rounded | | |
| | DI | | | |)() | |
| (b) | B1ft | Penalise rounding only once here. Condone 5.00 All points plotted within half of one square. Ft their values of y | | | | |
| (~) | 2220 | for $x = 2,3,4$ respectively | | | | |
| | B1ft | | All drawn points joined up in a smooth curve | | | |
| | | | | | | |
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| | | + | | → | | |
| | | - | | | | |
| (c) | M1 | For use of power law to obta | in log | $(6-2x)-\frac{1}{2}$ | $\pm x$ | |
| | IVII | For use of power law to obta | iii 10g ₃ | (0-2x)= | 4 | |
| | | | | + x | | |
| | M1 | For removing the \log_3 to obtain: $6-2x=3^{\frac{-1}{4}}$ Allow $(6-2x)^4=3^{\pm x}$ for this mark. | | | | |
| | | | | | | |
| | A1 | Υ π | | | | |
| | | For obtaining the equation $8-2x=3^{\frac{1}{4}}+2$ oe (eg., $-2x+8=2+3^{\frac{1}{4}}$) For drawing their straight line, provided it is of the form $y=k-2x$ where k | | | | |
| | | | ie, provi | ided it is of | the form y | $= \kappa - 2x$ where κ |
| | | is a constant. | | | | |
| | | | | | | |
| | | | | , | | |
| | | | | | | |
| | | | | | | |
| | M1 | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | H | | |
| | | [Check coordinates (1, 6) (2 | 2, 4) (| 3, 2) (4, 0) |)] | |
| | A 1 | For the intersection point (| r_) 2 1 | | | |
| | A1 | For the intersection point (| $\lambda - j = 2.1$ | | | |

| Question number | Scheme | Marks |
|--------------------|--|-----------|
| 8 | $\log_{1} a + 2\log_{1} b = \frac{5}{2}$ | M1 |
| | $\log_4 a + 2\log_4 b = \frac{5}{2}$ $\log_4 (ab^2) = \frac{5}{2}$ $32 = ab^2$ $2^a = \frac{2^{16}}{2^{2b^2}}$ | M1 |
| | $32 = ab^2$ | A1 |
| | $2^a = \frac{2^{16}}{2^{2b^2}}$ | M1 |
| | $a = 16 - 2b^2$ or $b^2 = 8 - \frac{1}{2}a$ | A1 |
| | $32 = a(8 - \frac{1}{2}a)$ or $32 = (16 - 2b^2)b^2$ | M1 |
| | $a^2 - 16a + 64 = 0$ or $2b^4 - 16b^2 + 32 = 0$ | A1 |
| | a=8 $b=2$ | A1 |
| | 1 ota | l 8 marks |

| Mark | Guidance |
|-----------|--|
| Log eq | uation Method 1 – Works in base 4 |
| M1 | For an attempt to change the base of $3\log_8 b$ to base 4 using $\log_a x = \frac{\log_b x}{\log_b a}$ |
| | $3\log_8 b = \frac{3\log_4 b}{\log_4 8} = \frac{3\log_4 b}{\frac{3}{2}} = 2\log_4 b$ [accept $p\log_4 b$ where $p \neq 3$] |
| | Uses $n \log A = \log A^n$ and $\log A + \log B = \log AB$ to combine the logs correctly |
| M1 | $\log_4(ab^2) = \frac{5}{2}$ [ft their <i>p</i> provided $p \neq 1$] |
| A1 | For removing the logs in the equation to obtain $32 = ab^2$ o.e. e.g. $a^2b^4 = 1024$ |
| | Method 2 – Works in base 8 |
| | For an attempt to change the base of $\log_4 a$ to base 8 using $\log_a x = \frac{\log_b x}{\log_b a}$ |
| M1 | $\log_4 a = \frac{\log_8 a}{\frac{2}{3}} = \frac{3\log_8 a}{2}$ [accept $q \log_8 a$ where $q \neq 1$] |
| | Uses $n \log A = \log A^n$ and $\log A + \log B = \log AB$ correctly to combine the logs |
| M1 | $\log_8(a^{\frac{3}{2}}b^3) = \frac{5}{2}$ [ft their q] |
| | |
| A1 | For removing the logs in the equation to obtain $a^{\frac{3}{2}}b^3 = 8^{\frac{5}{2}}$ and rearranges (raises |
| | both sides to the power of $\frac{2}{3}$) to obtain $32 = ab^2$ |
| Second | equation |
| | For attempting to change the second equation to powers of 2 or 4: |
| M1 | $2^{a} = \frac{2^{16}}{2^{2b^{2}}} \Longrightarrow \left[2^{a} = 2^{\left(16 - 2b^{2}\right)}\right] \text{ or } 4^{\frac{a}{2}} = \frac{4^{8}}{4^{b^{2}}} = \left(4^{\frac{a}{2}} = 4^{8 - b^{2}}\right)$ |
| | At least one correct change of term e.g either 2^{16} or 2^{2b^2} OR either $4^{\frac{a}{2}}$ or 4^8 |
| A1 | Combines the powers to achieve $a = 16 - 2b^2$ or $\frac{a}{2} = 8 - b^2$ oe |
| Attemp | t to solve the simultaneous equations |
| | For an attempt to solve their equations simultaneously, both of which must be in |
| M1 | terms of a and b^2 , to obtain a 3TQ in either a or b^2 . |
| | $32 = a(8 - \frac{1}{2}a) \Rightarrow a^2 - 16a + 64 = 0$ or $32 = (16 - 2b^2)b^2 \Rightarrow 2b^4 - 16b^2 + 32 = 0$ |
| M1 | For an attempt to solve their 3TQ in either a or b^2 by any method. See General Guidance for the definition of an attempt |
| | For example: |
| | $a^{2}-16a+64=0 \Rightarrow (a-8)(a-8)=0 \Rightarrow a=$ |
| | $2b^4 - 16b^2 + 32 = 0 \Rightarrow b^4 - 8b^2 + 16 = 0 \Rightarrow (b^2 - 4)(b^2 - 4) = 0 \Rightarrow b = \dots$ |
| A1 | For $a = 8$ and $b = 2$ [If $b = \pm 2$ is given as the final answer, withhold this mark]. |

| Question number | Scheme | Marks |
|--------------------|---|-----------|
| 9 (a) | $\frac{\mathrm{d}A}{\mathrm{d}t} = 0.03$ | В1 |
| | $A = \frac{1}{2}x^2 \sin 60^\circ = \frac{\sqrt{3}}{4}x^2$ | M1 |
| | $\frac{\mathrm{d}A}{\mathrm{d}x} = \frac{\sqrt{3}}{2}x$ | A1 |
| | When $x = 2$ $\frac{dx}{dt} = \frac{1}{\sqrt{3}} \times 0.03 = 0.0173 \text{ cm/s}$ | M1 A1 (5) |
| (b) | $V = \sqrt{3}x^3 \qquad \frac{\mathrm{d}V}{\mathrm{d}x} = 3\sqrt{3}x^2$ | M1 |
| | When $x = 2 \frac{dV}{dt} = 12\sqrt{3} \times 0.0173 = 0.36$ | M1 A1 (3) |
| | Tota | l 8 marks |

| Part | Mark | Guidance |
|------|------|---|
| (a) | B1 | For stating or using correctly in their Chain Rule $\frac{dA}{dt} = 0.03$ |
| | | For using the correct formula $\left(\frac{1}{2}ab\sin C\right)$ with the correct lengths and angle of 60° or $\frac{\pi}{3}$, for the cross-sectional area of the prism to |
| | M1 | obtain $A = \frac{1}{2}x^2 \sin 60^\circ = \left(\frac{\sqrt{3}}{4}x^2\right)$ and differentiating their expression which must be as a minimum $A = px^2$ to obtain $\frac{dA}{dx} = qx$ [where p and q are constants]. [The height of the triangle is $\frac{\sqrt{3}}{2}x$ if they use $\frac{1}{2} \times \text{base} \times \text{height}$] |
| | A1 | For the correct $\frac{dA}{dx} = \frac{\sqrt{3}}{2}x$ |
| | M1 | For applying a correct Chain rule using their $\frac{dA}{dx}$ and $x = 2$ to obtain $\frac{dx}{dt} = \left(\frac{1}{\frac{dA}{dx}} \times \frac{dA}{dt}\right) = \frac{dx}{dA} \times \frac{dA}{dt} = \frac{2}{\sqrt{3}} \times \frac{1}{2} \times 0.03$ |
| | A1 | $\frac{\mathrm{d}x}{\mathrm{d}t} = 0.0173$ |
| (b) | M1 | For a correct expression for the volume using their A from part (a) to obtain $V = \frac{\sqrt{3}}{4}x^2 \times 4x = \left(\sqrt{3}x^3\right)$ and differentiating their expression which must be as a minimum $V = mx^3$ to obtain as a minimum $\frac{dV}{dx} = nx^2$ [where m and n are constants] $\left(\frac{dV}{dx} = 3\sqrt{3}x^2\right)$ |
| | M1 | For applying a correct Chain rule using their $\frac{dV}{dx}$ and $x = 2$ to obtain $\frac{dV}{dt} = \frac{dV}{dx} \times \frac{dx}{dt} = 12\sqrt{3} \times 0.0173 = \begin{bmatrix} 0.359 \end{bmatrix} \text{(ft their } \frac{dx}{dt} \text{)}$ Note: $\frac{dx}{dt} = 0.0173 \text{ or } \frac{\sqrt{3}}{100}$ $\left(\frac{dV}{dt} = \frac{dV}{dx} \times \frac{dx}{dt} = 12\sqrt{3} \times \frac{\sqrt{3}}{100} = \frac{9}{25} = 0.36\right)$ For exact 0.36 |
| | A1 | For awrt 0.36 |

| Question number | Scheme | Marks |
|--------------------|---|----------|
| 10 (a) | $x = \tan^{-1}(-3) = -72$ | M1 |
| | $x = 108 \qquad x = 288$ | A1 A1 |
| | | (3) |
| (b) | $7\sin^2\theta + \sin\theta\cos\theta = 6(\sin^2\theta + \cos^2\theta)$ | M1 |
| | $\sin^2\theta + \sin\theta\cos\theta - 6\cos^2\theta = 0$ | |
| | $\frac{\sin^2\theta}{\cos^2\theta} + \frac{\sin\theta}{\cos\theta} - 6 = 0$ | 3.61 |
| | $\frac{1}{\cos^2\theta} + \frac{1}{\cos\theta} = 0$ | M1 |
| | $\tan^2\theta + \tan\theta - 6 = 0$ | A1 cso |
| | | (3) |
| (c) | $(\tan y + 3)(\tan y - 2) = 0$ | M1 |
| | $\tan y = -3 \qquad \tan y = 2$ | A1 |
| | y = 108,288 $y = 63,243$ | A1ft A1 |
| | | (4) |
| | Total | 10 marks |

| Part | Mark | Guidance |
|------------|--|--|
| (a) | | For using inverse tan to obtain any correct angle |
| | M1 | $\tan^{-1}(-3) \Rightarrow x = -71.565^{\circ}$ Accept awrt 72 ° |
| | | |
| | A1 | For either 108 or 288 |
| | A1 | For both 108 and 288 |
| (b) | Uses $\sin^2 \theta + \cos^2 \theta = 1$ on the given equation to obtain | |
| | IVII | $7\sin^2\theta + \sin\theta\cos\theta = 6(\sin^2\theta + \cos^2\theta)$ |
| | M1 | For rearranging and dividing through by $\cos^2 \theta$ with the $\frac{\sin \theta}{\cos \theta} = \tan \theta$ |
| | WII | identity to obtain a 3TQ: $\frac{\sin^2 \theta}{\cos^2 \theta} + \frac{\sin \theta}{\cos \theta} - 6 = 0 \Rightarrow \left(\tan^2 \theta + \tan \theta - 6 = 0\right)$ |
| | ALT | |
| | M1 | Divides the given equation through by $\cos^2 \theta$ with the $\frac{\sin \theta}{\cos \theta} = \tan \theta$ |
| | 1711 | identity to obtain $7 \tan^2 \theta + \tan \theta = \frac{6}{\cos^2 \theta}$ |
| | 3.54 | Uses $\sin^2 \theta + \cos^2 \theta = 1$ to obtain $\tan^2 \theta + 1 = \frac{1}{\cos^2 \theta}$ and uses this result on |
| | M1 | the given equation and rearranges to achieve a 3TQ to obtain |
| | | $7 \tan^2 \theta + \tan \theta = 6 (1 + \tan^2 \theta) \Longrightarrow (\tan^2 \theta + \tan \theta - 6 = 0)$ |
| | | |
| | A1 | For obtaining the given expression $\tan^2 \theta + \tan \theta - 6 = 0$ * in full. |
| | cso | Note: This is a show question, there must be no errors in the solution. |
| (c) | M1 | For changing $7\sin^2 y + \sin y \cos y = 6$ to $\tan^2 y + \tan y - 6 = 0$ [this step |
| | IVII | must be correct] and then attempting to solve the 3TQ by any method. |
| | A1 | For $\tan y = -3$ and $\tan y = 2$ |
| | A1ft | For both $y = 108$ and 288 (ft from (a)) |
| | A1 | For both $y = 63$ and 243 |
| Poun | ding or | Page: Panalice rounding only once in this question when first seen provided |

Rounding errors: Penalise rounding only once in this question when first seen provided angles round to 108, 288, 63 or 243

| Question number | Scheme | Marks |
|-----------------|---|-----------|
| 11 | $e^x = \frac{4}{e^x} \Longrightarrow e^{2x} = 4$ | M1 |
| | $x = \frac{1}{2} \ln 4$ or $x = \ln 2$ | A1 |
| | $\pi \int_0^{\ln 2} e^{2x} dx + \pi \int_{\ln 2}^a 16e^{-2x} dx$ | M1 M1 |
| | $\pi \left[\frac{1}{2} e^{2x} \right]_{0}^{\ln 2} + \pi \left[-8 e^{-2x} \right]_{\ln 2}^{a}$ | M1 |
| | $\pi \left(2 - \frac{1}{2}\right) + \pi \left(-8e^{-2a} + 2\right) =$ | M1 |
| | $\frac{7\pi}{2} - 8\pi e^{-2a} \qquad a = 2 \text{ and } k = \frac{7\pi}{2}$ | M1A1 |
| Total 8 ms | | l 8 marks |

| Mark | Guidance |
|-----------|---|
| M1 | Sets $e^x = \frac{4}{e^x}$ and attempts to make x the subject |
| | |
| | A minimum of $e^{2x} = 4$ or $e^x = 2$ is required to be seen for this mark. |
| A1 | For obtaining either $x = \frac{1}{2} \ln 4$ or $x = \ln 2$ |
| M1 | For stating $\pi \int_0^{\ln 2} (e^x)^2 dx = \pi \int_0^{\ln 2} e^{2x} dx$ using the limits of their ln 2 (which must |
| | be of the form $\ln k$) and 0 correctly |
| | Note: Condone a missing π here if it is seen at the final M mark. |
| M1 | For stating $\pi \int_{\ln 2}^{a} (4e^{-x})^2 dx = \pi \int_{\ln 2}^{a} 16e^{-2x} dx$ using a and the limit of their ln 2 |
| | (which must be of the form $\ln k$ where k is consistent between the two integrals) |
| | correctly Note: Condone a missing π if it is seen at the final M mark. |
| M1 | For an attempt to integrate both expressions obtaining: |
| | |
| | Either $\left \frac{e^{2x}}{2} \right $ or $\left \frac{-16e^{-2x}}{2} \right $ (condone $\left \frac{16e^{-2x}}{2} \right $) |
| | |
| | For this mark ignore the absence of π or incorrect/absent limits |
| | [need not be simplified] |
| dM1 | For substituting their limits correctly (where their ln 2 must be of the form ln k |
| | where k is consistent between the two integrals) into their integrated expression. For this mark ignore the absence of π |
| | |
| | $\pi \left(\frac{e^{2\ln 2}}{2} - \frac{e^0}{2} \right) + \pi \left(-16e^{-2a} - \frac{\left(-16e^{-2\ln 2} \right)}{2} \right) = \pi \left(2 - \frac{1}{2} \right) + \pi \left(-8e^{-2a} + 2 \right)$ |
| | This mark is dependent on the previous M mark. |
| M1 | For equating to the given expression for the volume and equating coefficients to |
| | find values for a and k. We must see π used here for the award of this mark. |
| | $\left(\pi\left(2-\frac{1}{2}\right)+\pi\left(-8e^{-2a}+2\right)=\frac{7\pi}{2}-8\pi e^{-2a}\right)$ |
| | $7\pi \qquad 8\pi e^{-2a} - k \qquad 8\pi e^{-4} \rightarrow k - a - a$ |
| | $\frac{7\pi}{2} - 8\pi e^{-2a} = k - 8\pi e^{-4} \Rightarrow k =, a =$ |
| A1 | For $a=2$ and $k=\frac{7\pi}{2}$ |
| | ۷ |